

Student name: Solution.

Calculators are allowed; a "cheat sheet" is on the other side

1. Solve for x : $\log_3(x+1) - \log_3(x) = 2$

$$\log_3\left(\frac{x+1}{x}\right) = 2$$

$$3^{\log_3\left(\frac{x+1}{x}\right)} = 3^2 = 9$$

$$x+1 = 9x \rightarrow \frac{x+1}{x} = 9$$

$$1 = 8x$$

$$x = \frac{1}{8}$$

Strategy: $\log_3(\quad) = \#$

$$3^{\log_3(\quad)} = 3^{\#}$$

$$(\quad) = 3^{\#}$$

2.

Growth of an Insect Population The size P of a certain insect population at time t (in days) obeys the function

$$P(t) = 500e^{0.02t}$$

$$A(t) = A(0)e^{kt}$$

a. What is the population after 0 days (that is, at the beginning)?

$$P(0) = 500$$

$$P(0) = 500e^{0.02 \cdot 0} = 500e^0 = 500$$

b. What is the population after 10 days?

$$P(10) = 500e^{0.02 \cdot 10} = 611 \text{ insects}$$

c. How long will it take for the population to double?

$$P(t) = 1000$$

$$1000 = 500e^{0.02t}$$

$$2 = e^{0.02t}$$

$$\ln(2) = 0.02t$$

$$t = \frac{\ln(2)}{0.02} = 34.66 \text{ days}$$

Strategy: $e^{(\quad)} = \#$

$$\ln e^{(\quad)} = (\quad) = \ln(\#)$$